## GCE

## Mathematics A

H240/03: Pure Mathematics and Mechanics

Advanced GCE

## Mark Scheme for June 2019

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

## Annotations and abbreviations

| Annotation in scoris | Meaning |
| :--- | :--- |
| $\checkmark$ and $\boldsymbol{x}$ |  |
| BOD | Benefit of doubt |
| FT | Follow through |
| ISW | Ignore subsequent working |
| M0, M1 | Method mark awarded 0, 1 |
| A0, A1 | Accuracy mark awarded 0,1 |
| B0, B1 | Independent mark awarded 0, 1 |
| SC | Special case |
| $\wedge$ | Omission sign |
| MR | Misread |
| Highlighting |  |
|  |  |
| Other abbreviations in |  |
| mark scheme | Meaning |
| E1 | Mark for explaining a result or establishing a given result |
| dep* | Mark dependent on a previous mark, indicated by * |
| cao | Correct answer only |
| oe | Or equivalent |
| rot | Rounded or truncated |
| soi | Seen or implied |
| www | Without wrong working |
| AG | Answer given |
| awrt | Anything which rounds to |
| BC | By Calculator |
| DR | This question includes the instruction: In this question you must show detailed reasoning. |

## Subject-specific Marking Instructions for A Level Mathematics A

a Annotations should be used whenever appropriate during your marking. The $A, M$ and $B$ annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. For subsequent marking you must make it clear how you have arrived at the mark you have awarded.
b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
If you are in any doubt whatsoever you should contact your Team Leader.
c The following types of marks are available.
M
A suitable method has been selected and applied in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A
Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B
Mark for a correct result or statement independent of Method marks.

E
Mark for explaining a result or establishing a given result. This usually requires more working or explanation than the establishment of an unknown result.
Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.
d When a part of a question has two or more 'method' steps, the $M$ marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only - differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case, please escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.
f Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km , when this would be assumed to be the unspecified unit.) We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so. When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case. When a value is not given in the paper accept any answer that agrees with the correct value to 3 s.f. Follow through should be used so that only one mark is lost for each distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examination.
g Rules for replaced work: if a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests; if there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others. NB Follow these maths-specific instructions rather than those in the assessor handbook.
$\mathrm{h} \quad$ For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question. Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working. 'Fresh starts' will not affect an earlier decision about a misread. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.
i If a calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.
j If in any case the scheme operates with considerable unfairness consult your Team Leader.


| 2 | (a) | (i) | $(x-3)^{2}-9+(y+2)^{2}-4+4=0 \Rightarrow(x-3)^{2}+(y+2)^{2}=9$ $C(3,-2)$ | M1 <br> A1 <br> [2] | 1.1 <br> 1.1 | $(x \pm 3)^{2}$ and $(y \pm 2)^{2}$ seen (or implied by correct answer) or one correct coordinate <br> Accept $x=3$ and $y=-2$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | (a) | (ii) | $r=3$ | $\begin{gathered} \text { B1 } \\ {[1]} \end{gathered}$ | 1.1 | Allow if stated explicitly in (a)(i) but not written down in (a)(ii) www for $r$ | B0 if $r= \pm 3$ only |
| 2 | (b) |  | $\begin{aligned} & (x-3)^{2}+(k x-3+2)^{2}=9 \text { or } \\ & x^{2}+(k x-3)^{2}-6 x+4(k x-3)+4=0 \\ & \left(1+k^{2}\right) x^{2}+(-6-2 k) x+1=0 \end{aligned}$ | M1* <br> A1 | 3.1a <br> 1.1 | Substitutes the correct equation of the line into any form of their equation of the circle <br> oe (all terms on the same side - may not be factorised but should be simplified to 5 terms) | Each M is dependent on the previous Ms <br> Condone lack of equal to 0 |
|  |  |  | $(-6-2 k)^{2}-4\left(1+k^{2}\right)(1)$ | M1dep* | 3.1a | Correct explicit use of discriminant on their 3TQ to get an expression in $k$ only | Condone equals or incorrect inequality |
|  |  |  | $36+24 k+4 k^{2}-4-4 k^{2}<0 \Rightarrow 32+24 k<0$ | M1dep* | 2.1 | Discriminant $<0$ and simplify to the form $a k+b<0$ (oe) | $a$ and $b$ non-zero |
|  |  |  | $k<-\frac{4}{3}$ | A1 <br> [5] | 2.2a | Fully correct (no additional values) | Or exact equivalent |


| Question |  | Answer | Marks | AO | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | (a) | DR <br> Attempt process for finding 2 critical values of $\|x-2\| \leq\|2 x-6\|$ | M1 | 1.1a | Either squaring both sides to obtain 3 terms on each side $\left(x^{2}-4 x+4 \leq 4 x^{2}-24 x+36\right)$ <br> simplifying and attempting to find two critical values (condone writing down roots from their quadratic without working) | Or attempt to solve 2 linear equations/inequalities, one with signs of $x$ and $2 x$ the same and the other with signs different (but condone other sign errors) |
|  |  | Obtain 4 <br> Obtain $\frac{8}{3}$ | A1 A1 | 1.1 1.1 | Award whether given as $x=4$ or $x \leq 4$ or $x \geq 4$ or $\ldots$ <br> Award whether given as $x=\frac{8}{3}$ or $x \leq \frac{8}{3}$ or $x \geq \frac{8}{3}$ or $\ldots$ |  |
|  |  | $x \geq 4 \text { or } x \leq \frac{8}{3}$ | A1 | 2.5 | Correct notation and must see 'or' (do not accept 'and' or a comma) - one or more strict inequality signs is A0 | Accept if in either correct set or interval notation e.g. $\begin{aligned} & \{x: x \geq 4\} \cup\left\{x: x \leq \frac{8}{3}\right\} \\ & \text { or }\left(-\infty, \frac{8}{3}\right] \cup[4, \infty) \end{aligned}$ |
|  |  |  |  |  |  | SC: If no DR (e.g. sketch and/or answers only) so M0 then award B1 only for both correct answers $x \geq 4$ or $x \leq \frac{8}{3}$ <br> (DR requires a detailed and complete analytical method) |
|  |  |  | [4] |  |  |  |


| 3 | (b) | Refers to translation and stretch <br> Either <br> State translation in (positive) $x$-direction by 4 (units) <br> State stretch by scale factor 0.5 in $x$-direction | M1 <br> A1 <br> A1 <br> [3] | 1.2 | In either order; ignore details here; allow any equivalent wording (such as move or shift for translation) to describe geometrical transformations but not statements such as add 4 to $x$ (do not accept 'enlargement' or ‘shear' for stretch) <br> Or state translation by $\binom{4}{0}$; accept horizontal to indicate direction or parallel to the $x$-axis; term 'translate' or 'translation' needed for award of A1 <br> Or parallel to $x$-axis or horizontally; term 'stretch' needed for award of A1; these two transformations must be in this order - if details correct for M1A1A1 but order wrong, award M1A1A0 | SC: if M0 but details of one correct (including correct order if req.), award B1 for $1 / 3$ (in Either, Or 1, Or 2 cases) <br> Do not accept ‘in/on/across /up/along the $x$ axis' or 'to the right' only A0 for SF 4 <br> Allow 'factor' or 'SF' for 'scale factor'. Do not accept 'in/ on/ across/ up/ along the $x$ axis', 'in the positive $x$-direction', 'SF 0.5 units' |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Or 1 State stretch by scale factor 0.5 in $x$-direction | A1 |  | or parallel to $x$-axis; 'stretch' needed for A1 |  |
|  |  | State translation in (positive) $x$-direction by 2 (units) | A1 [3] |  | Or state translation by $\binom{2}{0}$; these two transformations must be in this order - if details correct for M1A1A1 but order wrong, award M1A1A0 | Same conditions for Or 1 and Or 2 as for Either for acceptable terminology |
|  |  | Or 2 State translation in (positive) $x$-direction by 1 (unit) | A1 |  | Or state translation by $\binom{1}{0}$ or parallel to $x$ axis |  |
|  |  | State stretch by scale factor 2 in $y$-direction | A1 [3] |  | Or parallel to $y$-axis and allow vertical; term 'stretch' needed for award of A1; these two transformations can be given in either order | Do not accept ‘down’ only |




| 4 | (c) |  | $h=\frac{\pi}{8}$ | B1 | 1.1 | For using $\frac{1}{2} \times \frac{\pi}{8}$ or $\frac{\pi}{16}$ or exact equivalent or for stating $h$ | Not just for $\frac{\pi}{8}$ seen |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\begin{aligned} & \frac{1}{2} h\left[0+2\left(3\left(\frac{\pi}{8}\right) \sin \left(\frac{\pi}{4}\right)+3\left(\frac{\pi}{4}\right) \sin \left(\frac{\pi}{2}\right)+3\left(\frac{3 \pi}{8}\right) \sin \left(\frac{3 \pi}{4}\right)\right)+0\right] \\ & \left(=\frac{1}{2} h\left[0+2\left(\frac{3}{16} \pi \sqrt{2}+\frac{3}{4} \pi+\frac{9}{16} \pi \sqrt{2}\right)+0\right]\right) \end{aligned}$ | M1 | 2.1 | Correct [...] structure including multiplying the middle terms by 2 . The zeros may be omitted. Allow one incorrect $y$ value only. Any additional values or repeated values is M0. M0 if using $x$ values or if only non-exact values seen but allow for the M mark if left in terms of sin | Ignore $\frac{1}{2} h$ term for this mark <br> Note first 0 might be $3(0) \sin (2(0))$ and second 0 might be $3\left(\frac{\pi}{2}\right) \sin \pi$ |
|  |  |  | $\frac{1}{16} \pi\left(\frac{3}{8} \pi \sqrt{2}+\frac{3}{2} \pi+\frac{9}{8} \pi \sqrt{2}\right)$ | A1 | $1.1$ | Correct (possibly un-simplified) exact expression for integral | Not in terms of sin and correct value of $h$ used |
|  |  |  | $\frac{3}{32} \pi^{2}(\sqrt{2}+1)$ | A1 | 2.2a | $k=\frac{3}{32} \mathrm{www}$ |  |
|  |  |  |  | [4] |  |  |  |
| 4 | (d) | (i) | $\int_{0}^{\frac{1}{2} \pi} 3 x \sin 2 x \mathrm{~d} x=\frac{3}{4} \pi$ |  | 1.1 | BC - ignore any working and mark final answer only (allow awrt 2.36) | oe, e.g. 2.356... |
|  |  |  |  | [1] |  |  |  |
| 4 | (d) | (ii) | $\frac{3}{32} \pi^{2}(\sqrt{2}+1) \approx 2.23<2.356 \ldots$ so trapezium rule gives an under-estimate of the area | $\begin{aligned} & \text { B1 } \\ & {[1]} \end{aligned}$ | 2.2a | Dependent on correct value in (c) (but may not be exact) and correct value for integral in (d)(i) - must state in this part correct decimal values (to at least 2 sf ) for comparison (or 2.36 seen in (d)(i)) | B0 if only 'underestimate' stated with no reasoning |
| 4 | (d) | (iii) | LH trapezium above curve, but others below curve, so overall approximation not clear | B1 | 2.4 | oe e.g. trapezia/strips not all below the curve e.g. the curve changes from being convex to concave (concave up to concave down) e.g. the rate of change of the gradient changes from positive to negative | Condone mention of the curve being both concave and convex in the interval |



| 5 | (a) | DR $\begin{aligned} & (\cot \theta+\operatorname{cosec} \theta)^{2}=\left(\frac{\cos \theta}{\sin \theta}+\frac{1}{\sin \theta}\right)^{2} \\ & \text { or } \cot ^{2} \theta+2 \cot \theta \operatorname{cosec} \theta+\operatorname{cosec}^{2} \theta= \\ & \frac{\cos ^{2} \theta}{\sin ^{2} \theta}+2\left(\frac{\cos \theta}{\sin \theta}\right)\left(\frac{1}{\sin \theta}\right)+\frac{1}{\sin ^{2} \theta} \\ & =\left(\frac{1+\cos \theta}{\sin \theta}\right)^{2}=\frac{(1+\cos \theta)^{2}}{\sin ^{2} \theta}=\frac{(1+\cos \theta)^{2}}{1-\cos ^{2} \theta} \\ & \text { or } \frac{1+2 \cos \theta+\cos ^{2} \theta}{\sin ^{2} \theta}=\frac{1+2 \cos \theta+\cos ^{2} \theta}{1-\cos ^{2} \theta} \\ & =\frac{(1+\cos \theta)(1+\cos \theta)}{(1+\cos \theta)(1-\cos \theta)} \text { or } \frac{1+2 \cos \theta+\cos ^{2} \theta}{(1-\cos \theta)(1+\cos \theta)} \\ & =\frac{1+\cos \theta}{1-\cos \theta} \end{aligned}$ | M1* <br> M1dep* <br> M1dep* <br> A1 <br> [4] | 2.1 <br> 2.1 <br> 1.1 <br> 2.2a | Replace both cot and cosec correctly in terms of cos and $\sin$ or expands brackets and replaces all terms with correct expressions in terms of sin and cos <br> Combine terms and using $\sin ^{2} \theta=1-\cos ^{2} \theta$ correctly in denominator <br> Re-writes $1-\cos ^{2} \theta=(1+\cos \theta)(1-\cos \theta)$ <br> AG - correct proof - no notational or other errors such as missing $\theta^{\prime} s$ or inconsistent variables - must see $(1+\cos \theta)(1+\cos \theta)$ or $(1+\cos \theta)^{2}$ in numerator before AG | Allow omission of 2 if brackets expanded but must contain a $\cot \theta \operatorname{cosec} \theta$ term <br> Ignore terms in numerator for this mark <br> Dependent on both previous M marks |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | ALT | $\frac{1+\cos \theta}{1-\cos \theta}=\frac{(1+\cos \theta)(1+\cos \theta)}{(1-\cos \theta)(1+\cos \theta)}$ | M1* |  | Multiplying numerator and denominator by $(1+\cos \theta)$ |  |
|  |  | $\frac{(1+\cos \theta)^{2}}{1-\cos ^{2} \theta}=\frac{(1+\cos \theta)^{2}}{\sin ^{2} \theta}$ | M1dep* |  | Expanding and using $\sin ^{2} \theta=1-\cos ^{2} \theta$ correctly in denominator | Ignore numerator for this mark |
|  |  | $\left(\frac{1+\cos \theta}{\sin \theta}\right)^{2}=\left(\frac{1}{\sin \theta}+\frac{\cos \theta}{\sin \theta}\right)^{2}$ | M1dep* |  | Rewrite as a single squared term and split up into two terms | Dependent on both previous M marks |
|  |  | $=(\cot \theta+\operatorname{cosec} \theta)^{2}$ | A1 [4] |  | AG - allow candidates to 'meet in the middle' but for the A1 mark they must give a conclusion (e.g. 'LHS = RHS' or 'proved') |  |

5 (b)


(nan

\begin{tabular}{|c|c|c|c|c|c|c|}
\hline 8 \& (a) \& \(s=4 d\) \& \[
\begin{aligned}
\& \text { B1 } \\
\& {[1]}
\end{aligned}
\] \& 1.1 \& \& \\
\hline 8 \& (b) \& \[
\begin{aligned}
\& 2.4 U-\frac{1}{2} g \times 2.4^{2}=0 \\
\& U=11.76 \mathrm{~m} \mathrm{~s}^{-1}
\end{aligned}
\] \& \begin{tabular}{l}
M1 \\
A1 \\
[2]
\end{tabular} \& 3.3
\[
1.1
\] \& \begin{tabular}{l}
Use of \(s=u t+\frac{1}{2} a t^{2}\) correctly with \(s=0\), \(a= \pm g\) and time equal to 2.4 or \(v=u+a t\) with \(t=1.2, v=0\) and \(a= \pm g\) \\
Accept \(1.2 g\) or awrt 11.8 (accept -11.76 )
\end{tabular} \& \begin{tabular}{l}
oe use of other suvat equation(s) but must be a complete method to find \(U\) \\
From - \(g\)
\end{tabular} \\
\hline 8 \& (c) \& \[
\begin{aligned}
\& d=\left(\frac{5}{3} d\right) t \\
\& h=U t-\frac{1}{2} g t^{2} \\
\& h=5.292 \mathrm{~m}
\end{aligned}
\] \& \begin{tabular}{l}
B1 \\
M1 \\
A1 \\
[3]
\end{tabular} \& \begin{tabular}{l}
1.1 \\
3.3 \\
1.1
\end{tabular} \& \begin{tabular}{l}
oe - where \(t\) is the time for \(P\) to reach the wall \\
Use of \(s=u t+\frac{1}{2} a t^{2}\) correctly with \(a= \pm g\) and their \(U, t\left(h=11.76(0.6)-0.5(9.8)(0.6)^{2}\right)\) \\
Accept 5.29
\end{tabular} \& \begin{tabular}{l}
\[
\text { e.g. } t=0.6
\] \\
M0 if their \(t\) is 2.4 or 1.2 or if their \(U\) is \(5 d / 3\) (or in terms of d), M0 if \(t=\mathrm{f}(d)\) \\
Not 5.30
\end{tabular} \\
\hline 8 \& (d) \& \[
\begin{aligned}
\& v_{1}=U-g t \text { or } v_{1}^{2}=U^{2}-2 g h \\
\& \sqrt{\left(\frac{5}{3} d\right)^{2}+\left('^{\prime}-9.8 \times^{\prime} t^{\prime}\right)^{2}}(=16) \\
\& \sqrt{\left(\frac{5}{3} d\right)^{2}+\left(11.76^{\prime}-9.8 \times 0.6\right)^{2}}=16 \\
\& d=8.93
\end{aligned}
\] \& \begin{tabular}{l}
M1* \\
M1dep* \\
A1ft \\
A1 \\
[4]
\end{tabular} \& 3.3

3.4
1.1

1.1 \& \begin{tabular}{l}
Use of a correct suvat equation(s) to find the vertical speed $v_{1}$ at the top of the wall using either their $U$ and $t$ or their $U$ and $h$ For reference: $\left(v_{1}=11.76-g(0.6)\right.$ or $v_{1}^{2}=11.76^{2}-2 g(5.292)$ ) - may be seen in expression for speed <br>
Setting up an expression of the correct form for the speed or the speed squared in terms of $d$ only (using their $v_{1}$ ) <br>
'Correct' equation in $d$ following through their value for $U$ (and $h$ ) only <br>
Accept 8.92 (from using 11.8) www

 \& 

For reference $v_{1}=5.88$ <br>
M0 if vertical speed or $U$ is in terms of $d$ <br>
All other terms must be correct <br>
8.928225 80...
\end{tabular} <br>

\hline
\end{tabular}




| 10 | (c) | $t=1, \mathbf{s}=-\frac{1}{2} \mathbf{i}+(1+q) \mathbf{j}$ | M1* | 3.4 | Substitute $t=1$ into their $\mathbf{s}$ | Dependent on first M mark in (b) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $k\left(-\frac{1}{2} \mathbf{i}+(1+q) \mathbf{j}\right)=2 \mathbf{i}-8 \mathbf{j} \Rightarrow k=\ldots$ | M1dep* | 3.1b | Correct method in an attempt to find $q$ (e.g. equating a scalar multiple of their $\mathbf{s}$ (evaluated at $t=1$ ) to $2 \mathbf{i}-3 \mathbf{j}$ and solving for the scalar) |  |
|  |  | $k=-4 \Rightarrow q=1$ | A1 | 2.2a | www |  |
|  |  |  | [3] |  |  |  |



| 11 | (c) | $\frac{11}{24}(a+2 d) \leq a$ <br> $d \leq \frac{13}{22} a$ so greatest possible value of $d$ is $\frac{13}{22} a$ | M1 <br> A1 <br> [2] | 3.1b 2.2a | Uses the condition that $h$ cannot exceed $2 a \sin 30(=a)$ - allow if in terms of $k$ or their incorrect $k$ (e.g. $k(a+2 d)=a$ is M1) <br> Allow $d \leq \frac{13}{22} a$ or $d=\frac{13}{22} a$ | Allow any inequality sign or equals <br> A0 if exact answer not seen |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | (d) | e.g. model the ladder as non-uniform e.g. include a frictional component for the contact of the ladder with the wall <br> e.g. consider the size of the object at $C$ <br> e.g. consider the thickness of the ladder <br> e.g. consider the fact that the ladder could bend | B1 [1] | 3.5c | B0 if suggestion is to model the ground as smooth <br> B0 for using a more accurate value for $g$ |  |

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